

[Home](#) > A rotor having the following properties.....

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Question:

A rotor having the following properties :

$$m_1 = 4 \text{ kg}$$

$$\theta_1 = 45^\circ$$

$$r_1 = 75 \text{ mm}$$

$$m_2 = 3 \text{ kg}$$

$$\theta_2 = 135^\circ$$

$$r_2 = 85 \text{ mm}$$

$$m_3 = 2.5 \text{ kg}$$

$$\theta_3 = 240^\circ$$

$$r_3 = 50 \text{ mm}$$

Determine the amount of the counter mass at a radial distance of 75 mm required for the static balance.

Answer:

Data :

$$\begin{array}{llll}
 m_1 = 4 \text{ kg} & r_1 = 75 \text{ mm} & \theta_1 = 45^\circ & m_1 r_1 = 300 \text{ kg-mm} \\
 m_2 = 3 \text{ kg} & r_2 = 85 \text{ mm} & \theta_2 = 135^\circ & m_2 r_2 = 265 \text{ kg-mm} \\
 m_3 = 2.5 \text{ kg} & r_3 = 50 \text{ mm} & \theta_3 = 240^\circ & m_3 r_3 = 125 \text{ kg-mm}
 \end{array}$$

Radius of balance mass = $r = 75 \text{ mm}$

Let m = Balancing mass

Resolving horizontally,

$$\begin{aligned}
 \sum H &= m_1 r_1 \cos \theta_1 + m_2 r_2 \cos \theta_2 + m_3 r_3 \cos \theta_3 \\
 &= 300 \cos 45^\circ + 265 \cos 135^\circ + 125 \cos 240^\circ \\
 &= -37.87 \text{ kg-mm} \quad [1 \text{ M}]
 \end{aligned}$$

Resolving vertically,

$$\begin{aligned}
 \sum V &= m_1 r_1 \sin \theta_1 + m_2 r_2 \sin \theta_2 + m_3 r_3 \sin \theta_3 \\
 &= 300 \sin 45^\circ + 265 \sin 135^\circ + 125 \sin 240^\circ \\
 &= 291.25 \text{ kg-mm} \quad [1 \text{ M}]
 \end{aligned}$$

$$\begin{aligned}
 \text{Resultant } R &= \sqrt{(\sum H)^2 + (\sum V)^2} \\
 &= \sqrt{(-37.87)^2 + (291.25)^2} \\
 &= 293.70 \text{ kg-mm}
 \end{aligned}$$

We know that

$$m \times r = R$$

$$m = \frac{293.70}{75} = 3.91 \text{ kg} \quad \text{.....counterbalance mass} \quad [2 \text{ M}]$$
